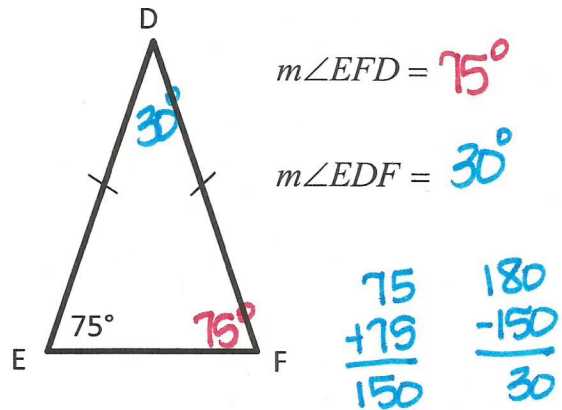
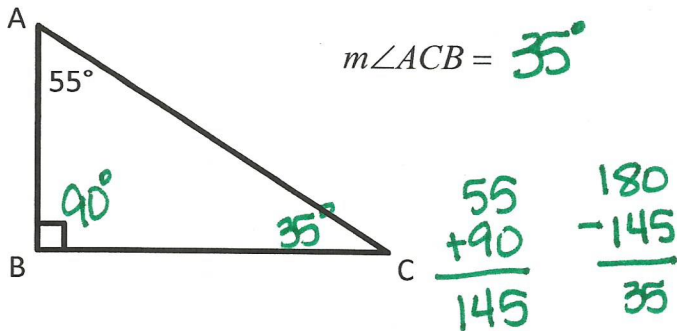


Lesson 19 Notes: Angle/Triangle Relationships

SUM OF THE ANGLES IN A TRIANGLE.

- the angles in a triangle ALWAYS add up to 180°.

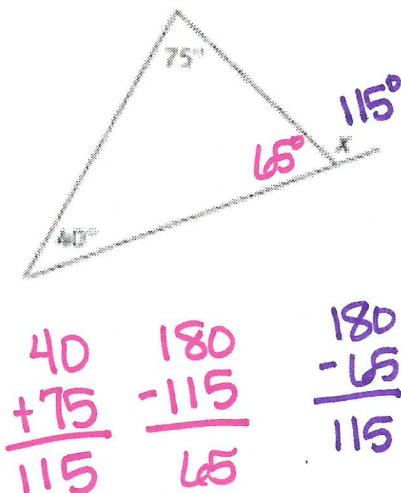
Find the missing angle measures.



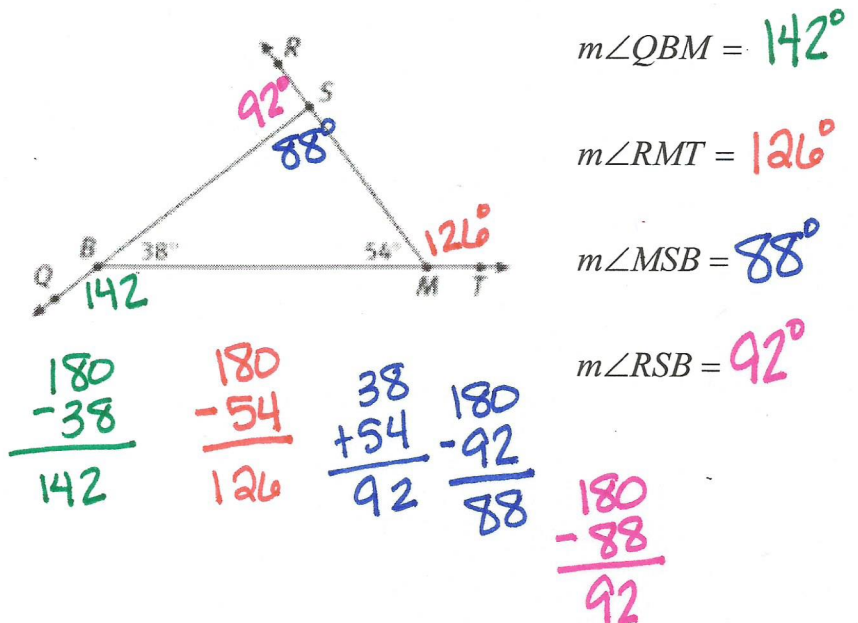
EXTERIOR ANGLES OF A TRIANGLE.

- when the side lengths of a triangle are extended, it creates exterior angles.
- The exterior angle and the angle that is adjacent to it are Supplementary, which means that they add up to 180°.

Find the value of x.



Find each of the missing angles.



$$m\angle QBM = 142^\circ$$

$$m\angle RMT = 126^\circ$$

$$m\angle MSB = 88^\circ$$

$$m\angle RSB = 92^\circ$$

Segment AC was drawn to create triangle ABC.

$$m\angle ACB = 58^\circ$$

$$32 + 90 = 122$$

$$180 - 122 = 58$$

Draw segment CD.

$$m\angle CAD = 58^\circ$$

$$90 - 32 = 58$$

$$m\angle ACD = 43^\circ$$

$$m\angle ADC = 79^\circ$$

$$58 + 43 = 101$$

$$180 - 101 = 79$$

Draw segment CF

$$m\angle FDC = 101^\circ$$

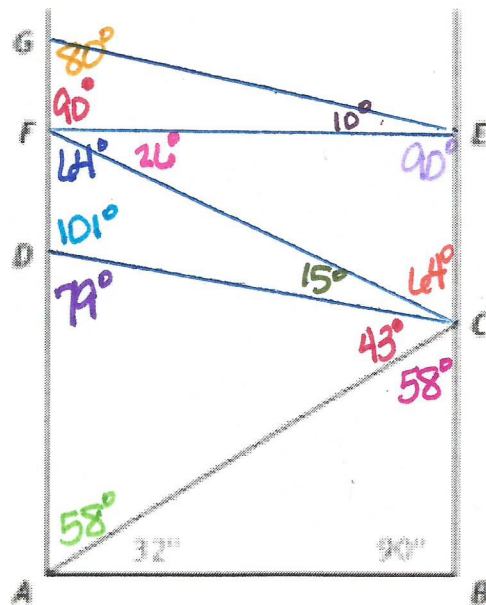
$$180 - 79 = 101$$

$$m\angle FCD = 15^\circ$$

$$m\angle DFC = 64^\circ$$

$$101 + 15 = 116$$

$$180 - 116 = 64$$



Draw segment FE

$$m\angle FCE = 64^\circ$$

$$15 + 43 + 58 = 116$$

$$m\angle FEC = 90^\circ$$

$$180 - 116 = 64$$

$$m\angle EFC = 26^\circ$$

$$90 + 64 = 154$$

$$180 - 154 = 26$$

Draw segment EG

$$m\angle GFE = 90^\circ$$

$$64 + 26 = 90$$

$$m\angle GEF = 10^\circ$$

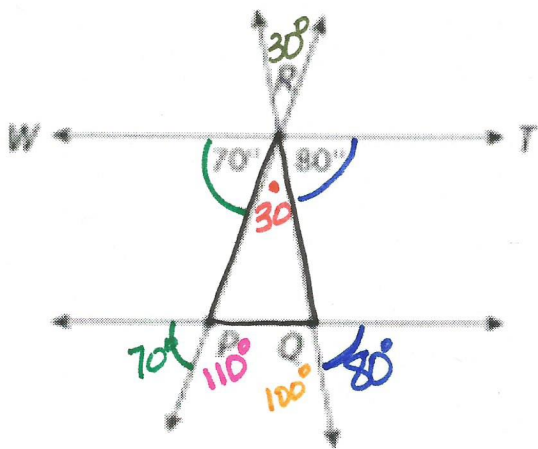
$$180 - 90 = 90$$

$$m\angle EGF = 80^\circ$$

$$90 + 10 = 100$$

$$180 - 100 = 80$$

Use your knowledge of lines, angles, and triangles to find the measure of angle P, Q, R.



$$m\angle R = 30^\circ$$

$$m\angle P = 110^\circ \quad 180 - 70 =$$

$$m\angle Q = 100^\circ$$

$$180 - 80 = 100$$

$$180 - 150 = 30$$

$$70 + 80 = 150$$

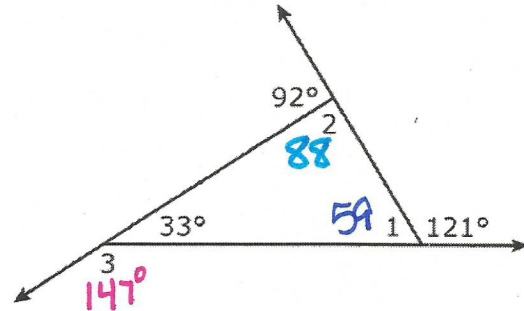
Guided Practice:

Use the diagram to find each angle measure.

1. angle 1 = 59° $180 - 121 = 59$

2. angle 2 = 88° $180 - 92 = 88$

3. angle 3 = 147° $180 - 33 = 147$



Use the diagram to find each missing measure.

4. angle x = 43° $180 - 137 = 43$

5. angle y = 123° $43 + 57 + x + 37 = 180$

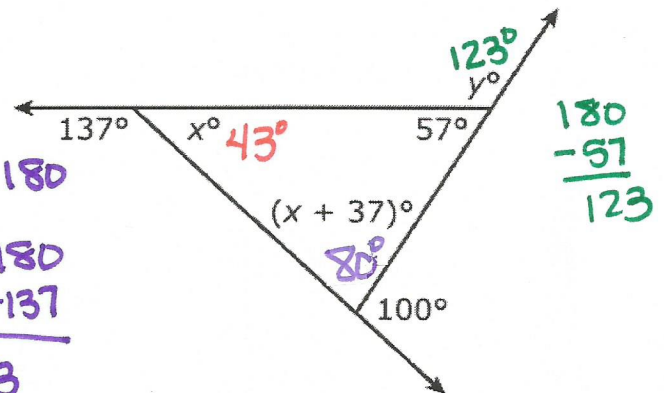
6. angle $(x+37) = 80^\circ$

$$\begin{array}{r} x + 137 = 180 \\ -137 \quad -137 \\ \hline x = 43 \end{array}$$

$$x = 43$$

$$x + 37$$

$$43 + 37 = 80^\circ$$



7. Lines c and d are parallel. The measure of angle 2 is 40° and the measure of angle 3 is 30° . What is the measure of angle 1?

$$\angle 1 + \angle 2 + \angle 3 = 180$$

$$\angle 1 + 40 + 30 = 180$$

$$\begin{array}{r} \angle 1 + 70 = 180 \\ -70 \quad -70 \\ \hline \angle 1 = 110^\circ \end{array}$$

$$\boxed{\angle 1 = 110^\circ}$$

