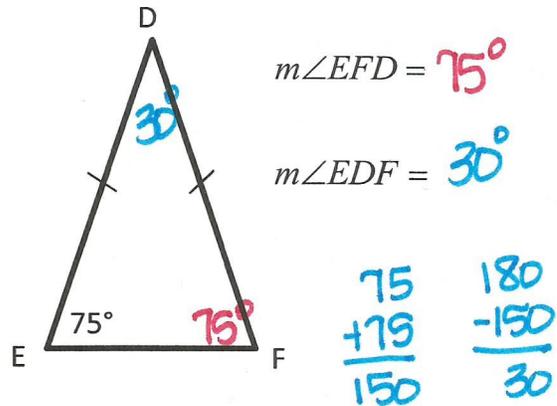
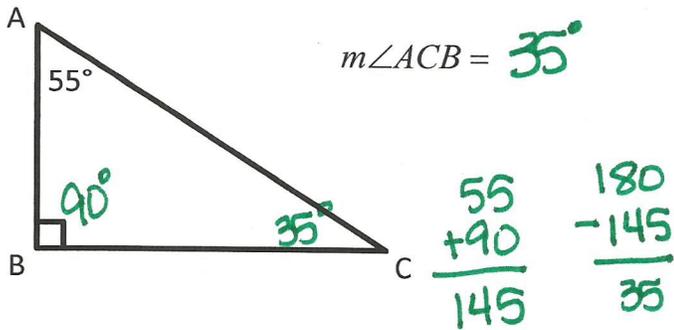


Lesson 19 Notes: Angle/Triangle Relationships

SUM OF THE ANGLES IN A TRIANGLE.

- the angles in a triangle ALWAYS add up to 180°.

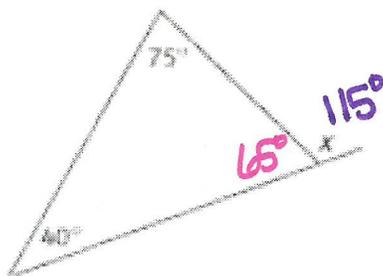
Find the missing angle measures.



EXTERIOR ANGLES OF A TRIANGLE.

- when the side lengths of a triangle are extended, it creates exterior angles.
- The exterior angle and the angle that is adjacent to it are Supplementary, which means that they add up to 180°.

Find the value of x.

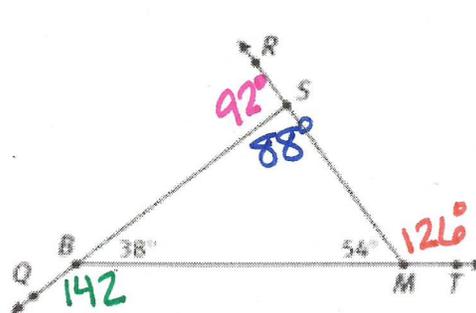


$$\begin{array}{r} 40 \\ +75 \\ \hline 115 \end{array}$$

$$\begin{array}{r} 180 \\ -115 \\ \hline 65 \end{array}$$

$$\begin{array}{r} 180 \\ -65 \\ \hline 115 \end{array}$$

Find each of the missing angles.



$$\begin{array}{r} 180 \\ -38 \\ \hline 142 \end{array}$$

$$\begin{array}{r} 180 \\ -54 \\ \hline 126 \end{array}$$

$$\begin{array}{r} 38 \\ +54 \\ \hline 92 \end{array}$$

$$\begin{array}{r} 180 \\ -92 \\ \hline 88 \end{array}$$

$m\angle QBM = 142^\circ$
 $m\angle RMT = 126^\circ$
 $m\angle MSB = 88^\circ$
 $m\angle RSB = 92^\circ$

$$\begin{array}{r} 180 \\ -88 \\ \hline 92 \end{array}$$

Segment AC was drawn to create triangle ABC.

$$m\angle ACB = 58^\circ \quad \begin{aligned} 32 + 90 &= 122 \\ 180 - 122 &= 58 \end{aligned}$$

Draw segment CD.

$$m\angle CAD = 58^\circ \quad 90 - 32 = 58$$

$$m\angle ACD = 43^\circ$$

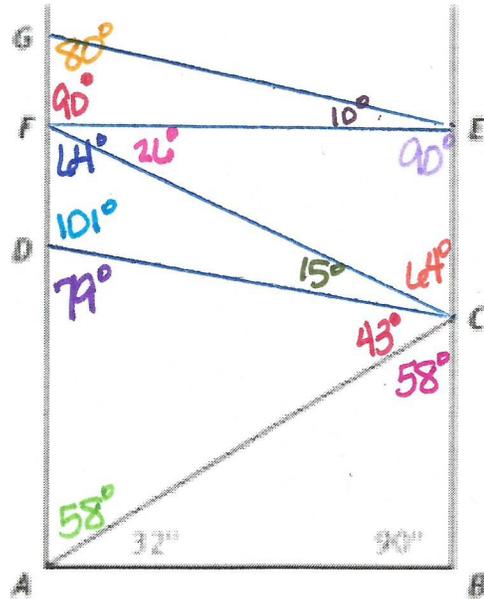
$$m\angle ADC = 79^\circ \quad \begin{aligned} 58 + 43 &= 101 \\ 180 - 101 &= 79 \end{aligned}$$

Draw segment CF

$$m\angle FDC = 101^\circ \quad 180 - 79 = 101$$

$$m\angle FCD = 15^\circ$$

$$m\angle DFC = 64^\circ \quad \begin{aligned} 101 + 15 &= 116 \\ 180 - 116 &= 64 \end{aligned}$$



Draw segment FE

$$m\angle FCE = 64^\circ \quad \begin{aligned} 15 + 43 + 58 &= 116 \\ 180 - 116 &= 64 \end{aligned}$$

$$m\angle FEC = 90^\circ$$

$$m\angle EFC = 26^\circ \quad \begin{aligned} 90 + 64 &= 154 \\ 180 - 154 &= 26 \end{aligned}$$

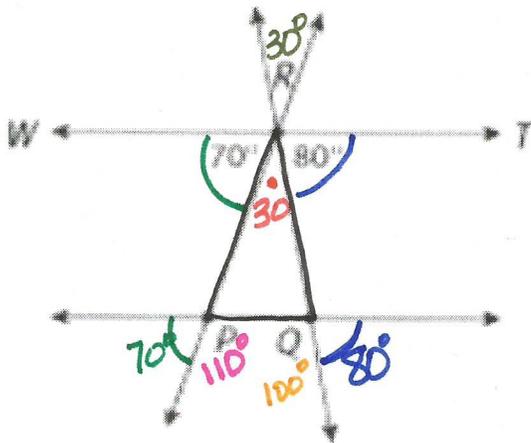
Draw segment EG

$$m\angle GFE = 90^\circ \quad \begin{aligned} 64 + 26 &= 90 \\ 180 - 90 &= 90 \end{aligned}$$

$$m\angle GEF = 10^\circ$$

$$m\angle EGF = 80^\circ \quad \begin{aligned} 90 + 10 &= 100 \\ 180 - 100 &= 80 \end{aligned}$$

Use your knowledge of lines, angles, and triangles to find the measure of angle P, Q, R.



$$m\angle R = 30^\circ$$

$$m\angle P = 110^\circ \quad 180 - 70 =$$

$$m\angle Q = 100^\circ \quad 180 - 80 = 100^\circ$$

$$180 - 150 = 30$$

$$70 + 80 = 150$$

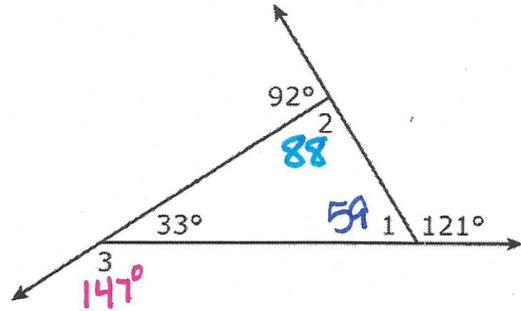
Guided Practice:

Use the diagram to find each angle measure.

1. angle 1 = 59° $180 - 121 = 59$

2. angle 2 = 88° $180 - 92 = 88$

3. angle 3 = 147° $180 - 33 = 147$



Use the diagram to find each missing measure.

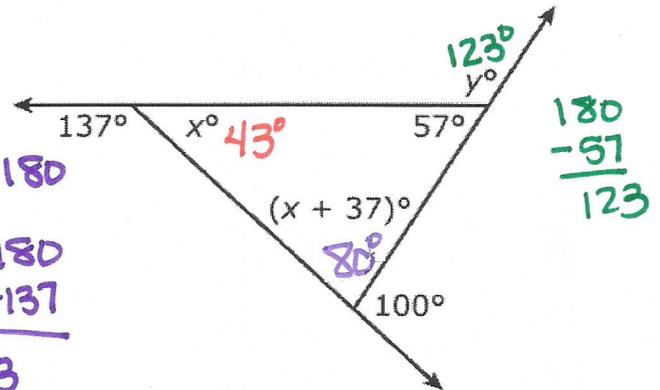
4. angle x = 43° $180 - 137 = 43$

5. angle y = 123° $43 + 57 + x + 37 = 180$

6. angle $(x+37) = 80^\circ$

$$\begin{array}{r} x + 137 = 180 \\ -137 \quad -137 \\ \hline x = 43 \end{array}$$

$$\begin{array}{r} x + 37 \\ 43 + 37 = 80 \end{array}$$



7. Lines c and d are parallel. The measure of angle 2 is 40° and the measure of angle 3 is 30° . What is the measure of angle 1?

$$\angle 1 + \angle 2 + \angle 3 = 180$$

$$\angle 1 + 40 + 30 = 180$$

$$\begin{array}{r} \angle 1 + 70 = 180 \\ -70 \quad -70 \\ \hline \end{array}$$

$$\boxed{\angle 1 = 110^\circ}$$

